### *Course: CSC14003 – Introduction to Artificial Intelligence*

### *Class 21CLC – Term II/2022-2023*

Homework 03

***Submission Notices:***

* *Conduct your homework by filling answers into the placeholders in this file (in Microsoft Word format).*

*Questions are shown in black color, instructions/hints are shown in italics and blue color, and your content should use any color that is different from those.*

* *After completing your homework, prepare the file for submission by exporting the Word file (filled with answers) to a PDF file, whose filename follows the following format,*

*<StudentID-1>\_<StudentID-2>\_HW01.pdf (Student IDs are sorted in ascending order)*

*E.g.,* ***2112001\_2112002\_HW02.pdf***

*and then submit the file to Moodle directly WITHOUT any kinds of compression (.zip, .rar, .tar, etc.).*

* *Note that you will get zero credit for any careless mistake, including, but not limited to, the following things.*
  1. *Wrong file/filename format, e.g., not a pdf file, use “-” instead of “\_” for separators, etc.*
  2. *Disorder format of problems and answers*
  3. *Conducted not in English*
  4. *Cheating, i.e., copying other students’ works or letting other students copy your work.*

**Problem 1. (3pts)** Consider a first-order knowledge base that describes worlds containing people, songs, albums (e.g., “Meet the Beatles”) and disks (i.e., particular physical instances of CDs). The vocabulary contains the following symbols:

* CopyOf(d, a): Disk d is a copy of album a
* Owns(p, d):Person p owns disk d
* Sings(p, s, a): Album a includes a recording of song s sung by person p
* Wrote(p, s): Person p wrote song s

Express the following statements in first-order logic:

1. Gershwin did not write “Eleanor Rigby.”
2. Either Gershwin or McCartney wrote “The Man I Love.”
3. Joe owns a copy of \*Revolver\*.
4. Every song that McCartney sings on \*Revolver\* was written by McCartney.
5. Gershwin did not write any of the songs on \*Revolver\*.
6. Every song that Gershwin wrote has been recorded on some album. (Possibly different songs are recorded on different albums.)
7. There is a single album that contains every song that Joe has written
8. Joe owns a copy of an album that has Billie Holiday singing “The Man I Love.”
9. Joe owns a copy of every album that has a song sung by McCartney. (Of course, each different album is instantiated in a different physical CD.)

*Please fill your answers in the table below*

|  |  |
| --- | --- |
| **No.** | **Original statements and FOL sentences** |
|  | Gershwin did not write “Eleanor Rigby.” |
|  |
|  | Either Gershwin or McCartney wrote “The Man I Love.” |
|  |
|  | Joe owns a copy of \*Revolver\*. |
|  |
|  | Every song that McCartney sings on \*Revolver\* was written by McCartney. |
|  |
|  | Gershwin did not write any of the songs on \*Revolver\*. |
|  |
|  | Every song that Gershwin wrote has been recorded on some album. (Possibly different songs are recorded on different albums.) |
|  |
|  | There is a single album that contains every song that Joe has written |
|  |
|  | Joe owns a copy of an album that has Billie Holiday singing “The Man I Love.” |
|  |
|  | Joe owns a copy of every album that has a song sung by McCartney. (Of course, each different album is instantiated in a different physical CD.) |
|  |

**Problem 2. (3pts)** **The Horned and Magical Unicorn.** If the unicorn is mythical, then it is immortal, but if it is not mythical, then it is a mortal mammal. If the unicorn is either immortal or a mammal, then it is horned. The unicorn is magical if it is horned. Prove by resolution that “the unicorn is both horned and magical.”

You are allowed to use these following propositional variables only

Y = unicorn is mYthical R = unicorn is moRtal M = unicorn is a maMmal

H = unicorn is Horned G = unicorn is magical

It is worth nothing that “immortal” = “not mortal”

*Please fill your answer in the following table.*

|  |  |  |  |
| --- | --- | --- | --- |
| **No.** | **Sentences** | | **Notes the sentence’s sources** |
| Translate the English sentences into propositional logic sentences | | | |
| 1. |  | | From the statement |
| 2. |  | | From the statement |
| 3. |  | | From the statement |
| 4. |  | | From the statement |
| 5. |  | | (need to be proven) |
| Convert propositional logic sentences into CNF | | | |
| 1. | |  |  |
| 2. | |  |  |
| 3. | |  |  |
| 4. | |  |  |
| 5. | |  |  |
| 6. | |  |  |
| 7. | |  | Negated goal |
| Resolution proof | | | |
| 8. | |  |  |
| 9. | |  |  |
| 10. | |  |  |
| 11. | |  |  |
| 12. | |  |  |
| 13. | |  |  |
|  | | *Add more rows if necessary* |  |

Conclusion: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

**Problem 3. (2pts)** Consider a vocabulary with the following symbols:

* In(a, b): predicate “a in b”
* Country(a): predicate “a is a country”
* Border(a, b): predicate “a border b”
* MapColor(a): predicate “Color of a in the map”

Translate each FOL sentence into natural language (English)

*Please fill your answers in the table below*

|  |  |
| --- | --- |
| **No.** | **Original statements and FOL sentences** |
| 1. | In(Paris,France) ∧ In(Marseilles,France) |
|  |
| 2. | ∃ c Country(c) ∧ Border (c,Iraq) ∧ Border (c,Pakistan) |
|  |
| 3. | ∀ c Country(c) ∧ Border (c,Ecuador ) ⇒ In(c, SouthAmerica) |
|  |
| 4. | ∀ c, d [In(c, SouthAmerica) ∧ In(d,Europe)] ⇒ ¬Borders(c, d)] |
|  |
| 5. | ∀ x, y (Country(x) ∧ Country(y) ∧ Borders (x, y) ∧ ¬(x = y)) ⇒ ¬(MapColor (x) = MapColor (y)) |
|  |

**Problem 4. (2pts)** Given a 3x3 grid of Sudoku game as below

|  |  |  |
| --- | --- | --- |
| 5 | 3 | a |
| 6 | b | c |
| 1 | 9 | 8 |

Suppose

* a1 is the logical variable that it is true then a is 1, else a is not 1
* a2 is the logical variable that it is true then a is 2, else a is not 2
* ….
* a9 is the logical variable that it is true then a is 9, else a is not 9
* Similar for b1, …, b2 and c1, …, c9.

1. Write CNF sentences to restrict available numbers for a, b, c using given logical variables. Each CNF sentence should go with a corresponding sentence in natural language. (1pt)

|  |  |
| --- | --- |
| **No.** | **CNF sentences** |
| 1. | *Your answer here* |
| 2. | *Your answer here* |
| 3. | *Your answer here* |
| 4. | *Your answer here* |
| 5. | *Your answer here* |
| 6. | *Your answer here* |
| … | *Your answer here* |

1. Find all sets of values for (a1, a2, …, a9), (b1, b2, …, b9), and (c1, c2, …, c9) that satisfies all CNF sentences in (a). Fill **T** **for True** and **leave blank for False** in the given table. (1pt)

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| a1 | a2 | a3 | a4 | a5 | a6 | a7 | a8 | a9 | b1 | b2 | b3 | b4 | b5 | b6 | b7 | b8 | b9 | c1 | c2 | c3 | c4 | c5 | c6 | c7 | c8 | c9 |
| - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - |
| - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - |
| - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - |
| - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - |
| - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - |
| - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - | - |